## A New Statistical Model of EEG Noise Spectra for Realtime, Low-γ-band SSVEP Brain-Computer Interfaces

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Introduction: A major impediment to practical real-time  $\gamma$ -band ( $\geq$  30Hz) SSVEP BCIs is the high level of spectral noise which dramatically increases the error rates of frequency detectors/estimators (Fig. 1a). The standard "1/*f*-type" spectral model [1] of EEG noise is both theoretically unsatisfactory and too ill-defined for hypothesis tests. Based on our new theory of *quantum ion channel kinetics* [2], we model EEG noise spectra as random processes of the form  $S_{\text{EEG}}(f) = S_{\text{GVZM}}(f) \cdot \Xi(f)$ , where  $\Xi(f)$  are independent  $\chi^2(2)/2$  random variables at each frequency f and  $S_{\text{GVZM}}(f)$  is the generalized van der Ziel-McWhorter deterministic function whose inverse Fourier transform is  $R_{\text{GVZM}}(t) = P_0 \int_{\tau_1}^{\tau_2} (1/\tau^{\alpha}) e^{-t/\tau} d\tau + P_1 \delta(t)$  for tunable parameters  $\alpha, \tau_1, \tau_2, P_0, P_1$  (Fig. 1b). We show such noise models have superior statistical characteristics for BCI and other neuroengineering applications.



*Figure 1.* (a) Raw single-trial EEG spectrum from 28Hz SSVEP BCI experiment showing a response peak which is nearly indistinguishable from background noise. (b) Synthetic GVZM  $\cdot \chi^2(2)/2$  noise spectrum optimally-fitted to the data of (a).

Figure 2. (a) Critical levels for SSVEP detection/estimation using standard smoothed periodogram algorithm [4] and the data of Fig.1. (b) Detection/estimation using optimally-fitted GVZM  $\cdot \chi^2(2)/2$  statistics.

*Material, Methods and Results:* The model was tested on a 15-second, 28Hz SSVEP trial (Fig. 1a) from a publically-available BCI dataset [3]. Biosemi electrodes A14-A16, A21-A23, A25, A27-A29 were averaged to form a virtual visual electrode. Blink artifacts were estimated by linear regression onto the three frontal electrodes. A popular *F*-test SSVEP detection algorithm [4] was compared to the same algorithm with its prestimulus estimator replaced by our optimally-fitted GVZM  $\cdot \chi^2(2)/2$  statistic. Each spectral value (excluding mid- $\alpha$ - and low- $\beta$ -bands) was classified with respect to its *F*-test critical value calculated from the null hypothesis

of no stimulus at that frequency. The results are shown in Fig. 2.

*Discussion:* The standard algorithm [4] failed to detect the 28Hz response spike in the noise background and also produced numerous false positives (Fig. 2a). On the other hand, our GVZM-based algorithm not only accurately detected the 28Hz response with P < .005, it also produced far fewer false positives (Fig. 2b).

Significance: This work proves that it is feasible to detect/estimate low- $\gamma$ -band SSVEP spikes in real-time despite their poor signal-to-noise characteristics by using neurologically-appropriate statistics for EEG background noise. Such noise models will be essential for the development of future practical real-time SSVEP BCIs in the mid- $\gamma$ -band.

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## References

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